Mission Matters
The Cost of Small High Schools Revisited

WORKING PAPER #08-03
March 2008

Leanna Stiefel
Wagner School
Institute for Education and Social Policy
New York University

Amy Ellen Schwartz
Institute for Education and Social Policy
Steinhardt and Wagner Schools
New York University

Patrice Iatarola
College of Education
Florida State University

Colin C. Chellman
Wagner School
Institute for Education and Social Policy
New York University
Acknowledgements

We thank the Carnegie Corporation for funding that supported this research. Sean Corcoran, William Duncombe, Henry Levin, Jennifer King Rice, Constancia Warren, Matthew Wiswall and seminar session participants at New York University’s Institute for Education and Social Policy, the University of Kentucky’s Martin School, and the American Education Finance Association’s 2007 annual meetings contributed helpful suggestions. All findings and opinions are our own. Authors listed in reverse alphabetical order.

Editorial Board

The editorial board of the IESP working paper series is comprised of senior research staff and affiliated faculty members from NYU's Steinhardt School of Culture, Education, and Human Development and Robert F. Wagner School of Public Service. The following individuals currently serve on our Editorial Board:

Amy Ellen Schwartz  
Director, IESP  
NYU Steinhardt and NYU Wagner

Sean Corcoran  
NYU Steinhardt

Cynthia Miller-Idriss  
NYU Steinhardt

Leslie Santee Siskin  
NYU Steinhardt

Leanna Stiefel  
Associate Director for Education Finance, IESP  
NYU Wagner

Mitchell L. Stevens  
NYU Steinhardt

Sharon L. Weinberg  
NYU Steinhardt

Beth Weitzman  
NYU Wagner
Abstract

With the financial support of several large foundations and the federal government, creating small schools has become a prominent high school reform strategy in many large American cities. While some research supports this strategy, little research assesses the relative costs of these smaller schools. We use data on over 200 New York City high schools, from 1996 through 2003, to estimate school cost functions relating per pupil expenditures to school size, controlling for school output and quality, student characteristics, and school organization. We find that the structure of costs differs across schools depending upon mission – comprehensive or themed. At their current levels of outputs, themed schools minimize per pupil costs at smaller enrollments than comprehensive schools, but these optimally-sized themed schools also cost more per pupil than optimally-sized comprehensive schools. We also find that both themed and comprehensive high schools at actual sizes are smaller than their optimal sizes.
Introduction

Reducing the size of high schools is a strategy popular among policymakers and philanthropists hoping to improve outcomes for students in urban school districts. In 2000, for example, the Oakland Unified School District began to develop ten new small high schools and Chicago opened 23 small high schools over the past few years (Oakland Unified School District, 2000; Gewertz, 2006). Additionally, in 2001, seven more districts across the country committed to creating small high schools and restructuring larger ones into multiple small schools with support from the Carnegie Corporation and the Gates Foundation.\textsuperscript{1} The small school reform model is clearly a popular solution to poor high school performance in large urban districts (Iatarola et. al., forthcoming).

At the same time, the substantial enthusiasm for small schools is not matched by a similarly substantial body of research demonstrating the effectiveness of reducing school size.\textsuperscript{2} While some research points to higher outcomes, it is not clear whether this is due to size or greater resources. Such research becomes increasingly important as the number of small high schools grows and as questions emerge about whether small schools can deliver improved student test scores better than larger high schools or, more fundamentally, whether and how size matters at all (Ravitch, 2006; Bloomfield, 2006; Viadero, 2006; Schneider et al, 2007). More importantly, as philanthropic resources decline, when policymakers allocate scarce public resources to diverse and numerous needs, we need to understand whether increasing the number of small schools is an effective use of those resources (Arenson, 2002).

Do smaller schools cost more or less? Is decreasing school size enough, or are other changes needed to transform failing comprehensive high schools into effective small schools? This paper continues a long

\textsuperscript{1} The initiative was named “New Schools for a New Society” and the seven districts - Boston, Chattanooga, Houston, Providence, Sacramento, San Diego and Worcester – each received $8 million for the initiative with the exception of Houston that received $12 million. The Carnegie Corporation and the Gates Foundation were joined by the Open Society Institute in spearheading a similar initiative in New York City – New Century High Schools – that was funded in 2001 at $30 million over five years (Carnegie Corporation of New York, 2006).

\textsuperscript{2} The definition of "small" varies significantly across the policy, advocacy/foundation, and empirical research literature. See Appendix A for the definitions of small, medium and large enrollment sizes referenced in prominent examples from the literature.
tradition in economics of estimating school cost functions (Cohn, 1968; Riew, 1966) and contributes to current research on the relationship between high school costs and size by examining the cost of schools using data on public high schools in New York City (NYC).

NYC is an especially appropriate location to study the cost-effectiveness of small high schools due, in large part, to its long-lived and vibrant small schools movement. Dating back to the 1960s, the first wave of small school reform focused on providing alternatives for students who were not succeeding in large and traditionally-oriented schools. The second wave of reform emerged in the mid-1990s, expanding the purview of small schools to a more academically oriented focus (Stiefel et al., 2000). The third and current wave of reform, by far the largest, promises to transform the landscape of secondary education in NYC, nearly doubling the number of high schools through the creation of small schools (Iatarola et al., forthcoming). Equally important, NYC has unusually rich data on its high schools including information on school expenditures, outputs, size, and characteristics of students, allowing us to construct a panel data set on over 200 high schools from 1995-96 to 2002-03 (hereafter 1996 to 2003).

This study improves on previous research examining the relationship between school costs and school size in six key ways. First, we use a larger sample of high schools than has previously been used, providing more statistical power; second, the variation in school size is considerably broader than previous studies ranging from fewer than 300 students to over 2,000 students; third, while previous research used only a single output measure -- the graduation rate, achievement test scores, or pass rates -- we include multiple measures of performance; fourth, while previous studies typically controlled for the “level” of outputs, we also include a measure of student performance prior to high school to estimate a “value-added” cost model; and fifth, we employ a longitudinal rather than cross-sectional design, which allows us to use panel data methods to control for unobserved school variables. Finally, we perform separate analyses for two types of high schools: themed schools, which range from small to medium size and provide narrowly focused curricula and course offerings, and comprehensive schools, which span a wide range of sizes and provide “…a variety of programs, support services and extra- and co-curricular
activities [with a…] full range of required and elective courses. While comprehensive schools are typically neighborhood-based schools, themed schools are not necessarily so and they address specific academic interests of students. In addition, themed schools are never large. Thus, we begin to disentangle the impacts of size and mission, often conflated in previous research.

Briefly, we find that the mission of a high school is important in determining its cost structure -- estimated cost parameters capturing the elasticity of costs with respect to size differ between these types of schools. The results suggest that for themed schools, costs per pupil decline with enrollment and are at their lowest at roughly 500 students. In contrast, for comprehensive schools, costs per pupil are still dropping at 500 and continue to drop through the largest observed size (around 4,000), although the marginal reductions are not substantively significant at the observed maximum. In addition, we find evidence that at current graduation rates and SAT scores, both types of high schools are, on average, too small. At higher output levels, however, costs are minimized for themed schools at considerably larger sizes than are currently typical.

Importantly, our results suggest that decreasing school size reduces costs only if small size is joined with themed mission. For example, our results show that transforming a 1,500 student comprehensive school into three 500 student comprehensive schools will likely increase costs without improving outcomes. On the other hand, if those three small schools become themed, it is possible to decrease costs per pupil.

The rest of this paper is organized as follows. In section two, we review the literature on the costs of schools of different sizes; in section three, we develop our conceptual framework and in section four, we describe our sample, data, and variables; in section five we present the study’s models and methods; in section six we describe results; and in section seven we discuss our findings and conclude.

4 Eighteen (out of 200) city high schools are vocational. Their mission and financing differ from comprehensive and themed and for that reason they are excluded from our analysis.
Previous Research

The debate about the relative merits of large and small high schools dates back at least a half a century to James Conant's (1959) support for the large comprehensive high schools developed at the turn of the 20th century. Since then, research has examined a wide range of issues related to school size, such as effects on outputs and outcomes, breadth and depth of curriculum, and social aspects of schools.\(^5\) Relatively little attention has been paid, however, to the relationship between school size and costs *per se* and the literature, which we review here, is fairly thin.

In an early paper, Riew (1966), using operating expenditure data on districts with a single high school, concluded that beyond an enrollment of 900, the existence of economies of scale is unclear. Cohn (1968) used district-level data on both short-run operating costs and long-run capital costs and found that the cost curve for high schools is U shaped, with the minimum cost at about 1,500 students suggesting rising per pupil costs beyond 1,500. Using only operating expenditures at the middle and elementary school level, Riew (1986) found declining costs in middle schools with enrollments as large as 1,024, but at the elementary school level the lowest costs he found were in schools with 200-400 enrolled students. In a more recent study of Welsh students aged 11 to 18, Foreman-Peck and Foreman-Peck (2006) find an optimum school size of 540 pupils, with schools over 600 pupils having lower exam scores and attendance rates, controlling for prior exam scores. Colgrave and Giles' (2005) recent meta-analysis of ten cost studies (some reviewed here) with 22 separate estimates concludes that the cost-minimizing high

\(^5\) Early empirical studies reveal a negative correlation between school size and academic outcomes, although costs are rarely included in these studies. For example, Fowler and Walberg (1991) and Fowler (1992) review literature that finds that students in small schools do better than those in large schools as measured by test scores, attendance rates, graduation or dropout rates, and participation in extracurricular activities. A more recent study that uses a NCES national database concludes that when output is measured as achievement in reading and math, the relationship between high school size and performance is U shaped with the optimal size between 600 and 900 or 1,200 students, depending on the subject and characteristics of the students (Lee and Smith, 1997). See Raywid (1996, 1999), Cotton (1996, 2001), Page et al. (2002) and Ready, Lee & Welner (2004) for a broader perspective on the research on school size.
school size is 1,540 students. All of the studies of high schools find a negative or flat relationship between size and average costs for high schools with enrollments up to around 1,000 students (see Chabotar, 1989; Watt, 1980; Kumar, 1983; and Bee and Dolton, 1985 for more results and Andrews et al., 2002, for a review of literature on the costs of different size districts and schools).

There are several common deficiencies in the existing studies of the effect of size on school costs. First, while understanding costs requires a simultaneous consideration of the quality and quantity of output, few existing studies do so. The empirical literature on costs often includes only one type of output and sometimes no outputs at all. To be specific, costs are likely determined by student performance, perhaps in multiple dimensions, as well as how many students are enrolled; costs are likely to be higher, ceteris paribus, when outputs are higher. Studies specifically relating costs to outputs suggest that small schools can be cost-effective. Stiefel et al. (2000) found costs of small high schools (less than 600 students) were about the same as large high schools when considered on a per graduate basis. Alternatively, in order to obtain exogenous variation in school size, Kuziemko (2006) examines shocks in enrollment in Indiana elementary schools and concludes that there are positive effects on math scores and attendance rates of moving to smaller size schools. Kuziemko estimates that roughly a 50% decrease in elementary school size led to a 20% increase in costs, but that the return on the additional costs yielded a net benefit of $3,298.

Second, the school is the appropriate unit of analysis to use in empirical work on school costs, but district-level data are often used, largely because school-level data are unavailable (for example, Cohn, 1968; Callan and Santerre, 1990). Third, cost functions rarely incorporate a value-added measure of output (Foreman-Peck and Foreman-Peck, 2006, are a recent exception), although such a measure is now commonplace in the production function literature and is the measure that corresponds best to the flow of costs per year. Finally, we should note that the available data measure public expenditures rather than costs. How -- and to what extent -- expenditures differ from costs (which, in principle, capture the minimum resources needed to produce a given output) is complicated by the presence of inefficiencies in production, among other concerns. We return to this below.
Our study improves on previous work by including several measures of outputs, incorporating a measure of lagged output and thus capturing value added, and focusing on schools as the unit of analysis.

**Conceptual Framework**

To fix ideas, a school-level education cost function captures the minimum resources needed to produce a set of constant quality outputs, given input prices and environmental and organizational features. In its general form, it can be represented as:

\[
C_{it} = g(q_{it}, p_{it}, n_{it}, e_{it}, o_{it})
\]

where \( c \) represents costs in school \( i \) at time \( t \), \( q \) represents outputs, \( p \) represents prices of inputs, \( n \) represents enrollment, \( e \) and \( o \) are environmental and organizational features, and \( g(.) \) is the functional form relating them. Note that the economic concept of cost in equation (1) is the minimum amount of resources (in dollars) used by each school to provide its outputs, which are different than expenditures. In this study, we use expenditure data, which is a measure of resources used, which will differ from costs if resources are not allocated to minimize costs.

Schools undoubtedly do not intend to minimize costs since they do not typically have an incentive or capacity to do so. Instead, the notion that schools act to maximize output given a budget constraint is more plausible. Notice then, that if the school district acts to minimize the total cost of all schools subject to a district output constraint (say, due to state standards), allocates resources accordingly, and schools act to maximize their own output subject to the resources given, then school resources may, in fact, reflect the minimum cost of producing the observed output.\(^6\) Unfortunately, it is unlikely that these conditions are a fully accurate description of the objectives and actions of the various administrators, superintendents and principals in a large district like NYC. Instead, the observed costs

\(^6\) Put differently, if the district acts to maximize output, subject to its budget constraint, allocates resources accordingly, and schools also act to maximize their output given their resources, the observed costs should be the minimum cost of producing the observed output.
also reflect differences in efficiency, or motivations, which we aim to control for using school fixed
effects, as discussed in more detail below.

Note that because cost functions specify output as a regressor, rather than as a dependent variable
as in a production function, multiple output measures can be included, which is especially important
because schools produce a variety of outputs. Environmental factors capture differences in the resources
needed to educate students with different needs. For example, poor students may have less well educated
parents who are unable to help them with homework or fewer educational resources available at home
such as books or computers, making the job of educating poor students more resource-intensive and hence
more costly than for comparable non-poor students. In addition to student characteristics, the cost
function includes features of the school organization, such as school type and, of course, school size,
which is our variable of primary interest.7

In this formulation, input prices and output quantities are exogenous. Notice, however, that the
prices of inputs (for example teacher salaries) are determined by district administrators rather than school
administrators and do not vary across schools within a district. That is, the schedule of salaries is the same
for all schools and, although there may be some differences in the prices of other inputs, within-district
differences in prices are likely to be small and relatively unimportant in the school budget. Salaries can,
and do, change over time as new contract terms apply and we capture these effects using year dummies.

Economic theory suggests several possible reasons that costs (measured per pupil) might vary
with school size or, put differently, that there may be economies or diseconomies of scale in schooling.
To begin, costs might decline with size as the fixed costs of schools are spread over a larger student body.
Fixed costs might include some aspects of the physical plant such as the gymnasium or cafeterias as well
as personnel, such as principals, or other inputs, such as library books. The key is that these inputs are, in
some measure, indivisible. Alternatively, economies of scale may reflect the gains from specialization

---

7 We do not include a measure of school efficiency because there is none. District-level measures such as data
envelopment analysis indices, generosity of resources, or competition indices such as the Herfindel index, do not
translate to the intra-district, school level. In addition, as discussed in the text, if schools act to maximize output
levels given a budget, then this produces the same result as cost-minimizing behavior.
and division of labor, for example, if teachers are able to specialize in offering courses in their areas of expertise. On the other hand, diseconomies of scale may set in at some point, due to limits to the ability of principals (or districts) to manage a large school or to congestion in the utilization of fixed resources. Which of these effects dominates is, essentially, an empirical matter.

Estimating this cost function requires data on school spending, student outcomes, and student and teacher characteristics, as well as information on environmental/neighborhood characteristics and organizational features of each school. In the absence of these data, school and borough fixed effects can be used to capture unobserved time-invariant characteristics of schools, their neighborhoods, organizational structure, and, potentially unobserved efficiency.

Data, Sample, and Measures

NYC provides a unique opportunity for studying small schools through the richness of data available as well as the scope of the small schools movement in the city. As the largest school system in the country, and also as part of the early 1990s small schools movement, NYC high schools offer a wider range of school sizes and student types than available elsewhere and over a longer period of time than used in other small schools cost studies. Data on school spending, student outcomes, and student and teacher characteristics are available for almost a decade, providing more statistical power for our analysis as well as more appropriate measures for a cost analysis.

Data

We obtained data from the NYC Department of Education (NYCDOE) based on school-based expenditure reports, cohort graduation reports, and high school report cards. School-Based Expenditure Reports (SBER) provide per-pupil expenditure information (for general education students), disaggregated into several functions and programs, for each high school for each year (see Appendix B.
for more detail) and, critical to this study, general education student enrollment. The cohort report data track students for four years from the point they enter the 9th grade, accounting for dropouts, transfers in and out of the school, and entrants to and withdraws from the system. Annual School Reports (ASRs) provide student demographic and test score data, teacher characteristics such as descriptions of teachers (e.g. percent with Masters’ degrees) and results of student performance on several Regents’ examinations, the New York State tests mandated for graduation. Below we provide detail on our sample of schools and important variables in our models.

Sample

This study uses a panel of data for a set of high schools serving 10th through 12th graders for the 1996 through 2003 graduating classes. In 2003, over 220 schools served nearly 300,000 high school students in New York City. We exclude specialized (magnet) high schools, vocational, “last chance,” or general equivalency diploma programs (GED). These schools have test-based admissions, do not assess progress in a standardized manner, or use alternative assessments of student progress (different graduation diplomas and/or high school tests) and thus they mostly have considerably less data available than the other types of high schools. We excluded all citywide special education schools, which are solely attended by full-time special education students. Taken together, all the excluded high schools represent approximately 24.4 percent of New York City high schools in 2003 but just 15.9 percent of high school students in that year. Put another way, in this study, we capture the majority of high school students and high schools that primarily educate general education students who are assessed in a standardized manner.

Over the years 1996 through 2003, we have data on 201 individual schools and 1,200 school-year observations.

---

8 The expenditure data were published for the first time in a comprehensive manner in 1996 – thus the need to begin no earlier than the graduating class of 1996 in this study. These data are unique to large city school districts in that they are detailed, well maintained and continuously available over an eight-year period.
9 “Last chance”/Transfer Alternative schools also address the needs of special populations, but students transfer into these schools in later grades, e.g., incarcerated students and pregnant teenagers. The General Education Diploma (GED) programs’ goal is for its enrolled students to attain a GED in situations where an alternative to a traditional high school diploma is necessary.
10 Citywide special education schools are those intended for student with severe disabilities. 5.7% (5.6%) percent of full-time special education students attend regular high schools over all the years in our sample (in 2003), but we do not include their expenditures and we do not include them in enrollment numbers.
Measures

We measure costs using data on modified direct expenditures, which represent resources used at the school level and include the inputs devoted to classroom instruction, instructional support services, leadership support, and ancillary support services (e.g., food service and school safety) but exclude building expenditures (e.g., energy and leasing costs), transportation and any of the district-level costs, such as the superintendent’s office or district debt service. Thus this measure captures resources used by the school itself to provide educational services and contains few allocated expenditures. Most importantly, building expenditures are excluded because they vary with the particular financial arrangement for the school building rather than resources devoted to learning. For example, many newer smaller schools are leased rather than owned outright; many older schools are fully depreciated and require more in energy and maintenance than newer buildings, but these added expenditures do not contribute to the educational function. Transportation expenditures are excluded as well because they capture neighborhood and geographic characteristics that are largely a function of whether a school is walking distance, accessible by subway or serves full-time special education students. Although the expenditure numbers cannot be regarded as perfectly capturing school costs of production, they are among the best school-level resource figures in the nation and offer the opportunity to shed light on the relationship between costs and school size. That said, while we use the terms costs and expenditures interchangeably in what follows, the underlying measures are based upon reported expenditures.

We measure school size as the enrollment of general education students, including those receiving part-time special education and other services. Following both the research literature and recommendations of school policymakers and advocates, we also distinguish five size categories, specifically very small (30 to 300 students), small (301 to 500), medium (501 to 1200), large (1201 to 2000) and very large (2,001 and larger). Appendix A more fully describes the rationale for these cut points.

11 Other alternative expenditure numbers, including total and instructional, behave similarly to modified and thus we do not show results using these other measures. The specific components of each measure are listed in appendix B.
Although often ignored in empirical work, high schools in NYC, as elsewhere, span a wide range of missions and goals, with corresponding differences in curricula, students and, in some measure, organizational and administrative structures within the Department of Education. We distinguish two non-overlapping categories of high schools – comprehensive and themed. Comprehensive high schools are traditional high schools that are typically neighborhood-based. They generally accept students based on geographic area of residence and do not require an entrance exam or audition. They usually provide several levels of difficulty for courses and multiple choices of languages and so on. Seventy-eight percent of the observations in our study belong to this category. \(^\text{12}\) Themed schools address the specific academic interests of students through special academic programs or themes, such as law, business, and health care, among others. This category includes the city’s official “small” schools – both, those formed over a decade ago in the first wave and new ones that are part of the second and current wave. The themed schools in total account for 22% of the observations in the sample.

We use multiple measures of high school outputs including average math and verbal scores on SAT examinations and SAT test-taking rates, in addition to the traditional four-year cohort graduation rates. \(^\text{13}\) Further, we include the percent of entering 9th grade students passing the state 8th grade math exam, which captures performance prior to entering high school to create a value-added specification. While inclusion of multiple outputs is realistic, the underlying production process is probably characterized by some degree of jointness in production. Put differently, the outputs may be jointly affected by changes in inputs and, as a result, independent variation is likely to be somewhat limited. As an example, increases in the SAT scores are likely related to increases in graduation rates; disentangling the separate impacts, \textit{ceteris paribus}, will be difficult and it is likely that the independent relationships

\(^\text{12}\) We report school-year observations for each type here, which are numbers of schools by type by year multiplied by the number of years in which a school appears.

\(^\text{13}\) Other output data, such as passing rates on Regents' exams (English and math) are available. We do not include these additional measures of outputs because of their high correlation with graduation rates and SAT scores and the likelihood that their inclusion would further limit the identification of independent relationships of the output variables to spending.
between outputs and costs will be inconsistently and imprecisely measured. Inclusion of multiple measures, however, will help minimize bias on estimates of the relationship between size and costs.

We include characteristics of a school’s student body that have been shown to influence the costs of education such as percent of students eligible for free lunch, limited English proficient and receiving “resource room” services (part-time special education services), as well as the racial composition of the student body.

While our data are relatively rich, New York City is physically and administratively large and culturally diverse, with each borough, neighborhood, and school having distinct characteristics unmeasured by the other variables. We attempt to control for these differences in a number of ways. Time fixed effects control for trends in spending and common changes in variables such as managerial efficiency system-wide or changes in standards, curricula, or budgeting. We begin by including borough fixed effects then estimate models using school fixed effects to capture unobserved time-invariant characteristics of schools. In this case, the size coefficients capture the direct impact of enrollment holding these unobserved time-invariant school characteristics fixed. Of course, some or all of these unobserved factors may well be due to the size itself and we might wish to include the impact of these factors in our estimates of the impact of size on costs. To do so, we also estimate our model using school random effects rather than fixed effects. Put differently, we may well wish to include the indirect effects of size as well as the direct effects, which a random effects specification allows. Further, using school fixed effects identifies impacts from changes in size within schools over time, which means that it relies upon a much smaller number of observations than the random effects allow. Finally, it is possible that the variation in size over time is non-randomly distributed across schools, which means that the fixed effects estimates may be misleading. Given the potential differences, we estimate the models using both random effects and fixed effects and find that the results are qualitatively and substantively similar.

---

14 All expenditures are in constant 2003 dollars that have been adjusted using CPI-U, Bureau of Labor Statistics. Thus, the time fixed effects do not also absorb inflationary increases in spending.
Descriptive Statistics

Table 1 displays descriptive statistics for all 180 high schools in our sample for 2003. To begin, costs per pupil averaged $8,205. The average high school in our sample enrolled 1,283 students, and the range is large, varying from 92 to 4,204 students. Twenty-eight percent of all schools are very large, 9% are large, 29% percent are medium-sized, 24% percent are small and 11% are very small. In the average high school, 58% of students graduate in four years and, of the roughly 37% of students who take the SAT, the average math and verbal score is 837. In the average high school, just over 17% of entering 9th graders passed standardized math exams in 8th grade and the student body includes 10% Asian, 40% black, 38% Hispanic, and 12% white, with slightly more female than male students (52% to 48%, respectively), 61% eligible for free lunch, 14% limited English proficient, 10% recent immigrant, and 6% in need of resource room services (part-time special education).

15 Indicators for missing data for independent variables are included in regression analyses, to maintain sample size, but the descriptive statistics are based on available data only.
As seen in Table 2, the distribution of schools across the sizes and types is quite uneven. While comprehensive high schools come in all sizes, ranging from the very small to the very large, themed high schools span a narrower range - from very small to medium. Viewed from the other perspective, small and very small schools are relatively evenly split between comprehensive and themed schools; a large
majority of medium schools are comprehensive and importantly, all large and very large schools are comprehensive schools. Thus, the observed variation in sizes across types is sufficient to allow us to gain some insight into the relationship between mission and size, but this variation is entirely within schools of medium-size and smaller.\textsuperscript{16}

\begin{table}
\centering
\begin{tabular}{lcccc}
\hline
 & \textbf{Comprehensive} & & \textbf{Themed} & \\
 & \textbf{Number} & \textbf{Percent} & \textbf{Number} & \textbf{Percent} \\
\hline
Very small (<300) & 8 & 5.8\% & 11 & 26.8\% \\
Small (301-500) & 21 & 15.1\% & 22 & 53.7\% \\
Medium (501-1,200) & 44 & 31.7\% & 8 & 19.5\% \\
Large (1,201-2,000) & 16 & 11.5\% & 0 & 0.0\% \\
Very large (2,000+) & 50 & 36.0\% & 0 & 0.0\% \\
\hline
Total & 139 & 100.0\% & 41 & 100.0\% \\
\hline
\end{tabular}
\caption{Crosstabulation of Schools by Size and Type, 2003}
\end{table}

\textbf{Models and Methods}

Estimating a cost function as in (1) proceeds, then, by specifying a functional form for the cost function. Unfortunately, theory and literature provide little guidance about the functional form of a school cost function and, thus, we explore two specifications, one with dichotomous and the other with continuous size variables. In addition, we also explore the differences in the cost functions between comprehensive and themed schools using both pooled regressions, which include high schools of both

\textsuperscript{16} Note that NYC does have several large high schools with specialized curricula, focusing on math and science or performing arts, which demonstrates that large size does not guarantee a comprehensive mission. Because these schools admit students based on admissions exams, we exclude them from our analytic sample.
types in a single regression, allowing for key coefficients to differ by type, and separate regressions, which allow for the full set of coefficients to vary by type.

Our first equation specifies size as a step function, with a series of dummy variables for size categories. This equation also includes indicators for the different high school mission types. This equation is as follows:

\[
\text{ln}\text{cost}_{it} = \beta_0 + \beta_1\text{Size}_{it} + \beta_2\text{Themed}_{it} + \beta_3\text{Output}_{it} + \beta_4\text{LagOutput}_{it} + \beta_5\text{Student}_{it} + \beta_6\text{Boro}_i
\]

\[+\beta_7\text{Year}_t + \varepsilon_{it}\]

where \(\text{ln}\text{cost}\) is the natural log of expenditure per general education pupil; \(\text{size}\) is one of five size dummy variables, described earlier; \(\text{Themed}\) is an indicator variable distinguishing themed schools from comprehensive high schools; \(\text{Output}\) includes the four year cohort graduation rate, SAT scores, and percent taking the SAT; \(\text{LagOutput}\) is the average eighth grade test score for the “graduating cohort” as they entered high school; \(\text{Student}\) is a series of variables capturing the characteristics of the student body such as the percentage eligible for free or reduced price lunch; \(\text{Boro}\) is a fixed effect for each of NYC’s five boroughs; \(\text{year}\) is a set of time fixed effects; \(\varepsilon\) is an error term with the usual properties and \(i\) indexes schools and \(t\) indexes school years.

To be clear, our central interest lies in estimating the coefficients on the size variables, which we interpret as estimates of the differences in the per pupil cost of education across the different school types. Other variables serve to control for other determinants of the cost of education. Notice that since costs are measured in natural logarithms, the coefficients will capture the percentage differences between these.

The second equation specifies size as a continuous variable and interacts size with mission type and final outputs:

\[
\text{ln}\text{cost}_{it} = \beta_0 + \beta_1\text{LnEnroll}_{it} + \beta_2\text{LnEnroll}_{it}^2 + \beta_3\text{Themed}_{it} + \beta_4\text{Themed}_{it}\text{LnEnroll}_{it}
\]

\[+\beta_5\text{Themed}_{it}\text{LnEnroll}_{it}^2 + \beta_6\text{Output}_{it} + \beta_7\text{Output}_{it}\text{LnEnroll}_{it} + \beta_8\text{LagOutput}_{it}
\]

\[+\beta_9\text{Student}_{it} + \beta_{10}\text{Boro}_i + \beta_{11}\text{Year}_t + \varepsilon_{it}\]

where \(\text{LnEnroll}\) is the natural logarithm of the number of general students enrolled and all other variables are the same as in equation 2. In addition, we substitute school fixed effects (random effects) for borough
fixed effects in some specifications. Here, our central concern is with estimating the relationship between costs and size and examining whether there are significant differences in the size relationship between themed and comprehensive high schools.\(^\text{17}\)

Our final analysis estimates separate cost functions for themed and comprehensive high schools, allowing each to have its own coefficients and size relationship.

\[
\text{lncost}_{it} = \beta_0^T + \beta_1^T \text{lnEnroll}_{it} + \beta_2^T \text{lnEnroll}_{it}^2 + \beta_6^T \text{Output}_{it} + \beta_7^T \text{Output}_{it} \text{lnEnroll}_{it} \\
+ \beta_8^T \text{LagOutput}_{it} + \beta_9^T \text{Student}_{it} + \beta_{10}^T \text{Boro}_{it} + \beta_{11}^T \text{Year}_{it} + \epsilon_{it}
\]

where \(T=\text{Themed or Comprehensive}\). Each of the equations (4) is estimated using a subsample of the high schools – either the themed or the comprehensive high schools.

**Results**

In this section, we first present the estimated cost functions and we then explore the implications of our estimates for optimal (cost minimizing) school size.

**Cost Function Estimates**

Table 3 presents the results of estimating cost functions using the dichotomous specifications of size as in equation (2). To begin, notice that the relationship between costs and the characteristics of the student body is consistent with expectations. Higher percentages of poor and of limited English proficient (LEP) students increase costs. *Ceteris paribus*, a ten percentage point increase in poor students

---

\(^{17}\) Notice that for comprehensive high schools the elasticity of costs with respect to size can be calculated as \(\beta_1 + 2\beta_2 \text{lnEnroll}_{it} + \beta_7 \text{Output}_{it}\). Thus, we allow the elasticity of cost to vary with both size and output level. Calculating this elasticity for themed schools requires adding in \(\beta_4 + 2\beta_5 \text{lnEnroll}_{it}\), allowing the cost elasticity to differ for themed and comprehensive schools, although the coefficients on other cost factors are held constant. The optimal size is found where this elasticity is zero, with second order conditions met.
raises per pupil costs by 0.5%; and such an increase in LEP and part-time special education students raises costs by 4.6% and 3.8%, respectively.\textsuperscript{18} Coefficients on other student characteristics, while consistent with expectations, are not statistically significant at the 5% level.

Table 3: Cost Regression Results, Dichotomous Size and Type Variables, All Schools, 1996 to 2003

<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficient (Robust Standard Errors)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant</td>
<td>8.5764*** (0.0410)</td>
</tr>
<tr>
<td>Size Categories</td>
<td></td>
</tr>
<tr>
<td>Small (301 - 500)</td>
<td>-0.1468*** (0.0263)</td>
</tr>
<tr>
<td>Medium (501 - 1,200)</td>
<td>-0.1512*** (0.0277)</td>
</tr>
<tr>
<td>Large (1,201 - 2,000)</td>
<td>-0.1984*** (0.0308)</td>
</tr>
<tr>
<td>Very large (2,001 +)</td>
<td>-0.2832*** (0.0308)</td>
</tr>
<tr>
<td>Themed</td>
<td>-0.0136 (0.0148)</td>
</tr>
<tr>
<td>% graduate, 4-year cohort</td>
<td>-0.0016*** (0.0004)</td>
</tr>
<tr>
<td>SAT score</td>
<td>-0.0000 (0.0001)</td>
</tr>
<tr>
<td>% taking SAT</td>
<td>0.0000 (0.0005)</td>
</tr>
<tr>
<td>% cohort passing Math, 8th grade</td>
<td>0.0006* (0.0003)</td>
</tr>
<tr>
<td>% Asian</td>
<td>-0.0005 (0.0008)</td>
</tr>
<tr>
<td>% black</td>
<td>0.0006* (0.0004)</td>
</tr>
<tr>
<td>% Hispanic</td>
<td>-0.0004 (0.0005)</td>
</tr>
<tr>
<td>% female</td>
<td>0.0010* (0.0006)</td>
</tr>
<tr>
<td>% eligible for free lunch</td>
<td>0.0005** (0.0002)</td>
</tr>
<tr>
<td>% limited English proficient</td>
<td>0.0046*** (0.0012)</td>
</tr>
<tr>
<td>% recent immigrants</td>
<td>-0.0032*** (0.0012)</td>
</tr>
<tr>
<td>% part-time special education</td>
<td>0.0038** (0.0019)</td>
</tr>
<tr>
<td>Observations</td>
<td>1200</td>
</tr>
<tr>
<td>R-squared</td>
<td>0.75</td>
</tr>
</tbody>
</table>

Dependent variable measured in natural logs. Model includes year effects and borough effects.
* significant at 10%; ** significant at 5%; *** significant at 1%
Indicators for missing independent variable data (not shown) are included in regression analyses.
Sample description: Specialized and Vocational schools removed as explained in the text, leaving two types of schools: Comprehensive and Themed. Omitted groups: Very Small size category; Comprehensive type category.

\textsuperscript{18} In contrast, increases of ten percentage points in recent immigrants lower costs per pupil by 3.2%. This latter result is consistent with work that finds, holding other characteristics constant, that immigrants perform better than native-born students in school (Schwartz and Stiefel, 2006).
The regressions indicate that, as anticipated, costs are monotonically decreasing in school size. Small schools cost almost 15% less than very small schools (the omitted category); medium size schools are slightly cheaper even; large size schools nearly twenty percent cheaper than very small schools and very large schools fully 28% cheaper than very small schools. Viewed somewhat differently, large schools are five percent cheaper than medium and small sized schools while very large schools are fifteen percent cheaper than medium and small sized schools. Thus, these results point to significant economies of scale. The specification of those relationships are, however, fairly restrictive.

Interestingly, themed schools do not seem to have significantly different costs from comprehensive schools, although, as shown in Table 2, mission and size are related - with themed schools relatively small and comprehensive schools all sizes. Interpreting the coefficients on outputs is more difficult, since the regressions include multiple output measures simultaneously. In principle, each coefficient captures the marginal cost of raising that single output, holding constant the quantities of the other outputs, and in general marginal costs should be positive. But, as pointed out earlier, both in theory and in practice, the output measures are likely to move together, making precise and consistent estimation of coefficients difficult. Interpreted literally, the results suggest that a ten percentage point increase in four-year cohort graduation rates reduces costs by 1.6%.

To explore these relationships in greater detail, we turn then to a more flexible specification, measuring size using enrollment and its square and allowing the impact of size to vary between themed and comprehensive schools by including an interaction term.19

The estimates in Table 4 are consistent with the predictions of theory and prior evidence. Although not shown in the table, the coefficients on poor, limited English proficient, and part-time special education students indicate that they are more costly to educate, while recent immigrants are cheaper.

---

19 An exploration of cubic terms indicated the quadratic is sufficient. Cubic terms were nearly uniformly insignificant.
As shown in Table 4, cost functions are U shaped with respect to size, with themed schools moving along a different and higher curve than comprehensive schools. That is, themed schools have higher fixed costs per pupil, with costs initially dropping more quickly (larger cost elasticity) than for comprehensive schools, then rising more rapidly. The cost of raising SAT scores is positive, although decreasing with school size, while increasing cohort graduation rates cost less, but that cost increases with size (although the coefficient is statistically insignificant). Costs per pupil decrease with higher percentages of students taking the SATs.

Table 4: Cost Regression Results, Continuous Size and Dichotomous Type and Size Interactions, All Schools, 1996 to 2003

<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficient (Robust Standard Errors)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant</td>
<td>10.0910*** (0.5055)</td>
</tr>
<tr>
<td>ln(Size)</td>
<td>-0.4170*** (0.1459)</td>
</tr>
<tr>
<td>[ln(Size)]²</td>
<td>0.0239** (0.0105)</td>
</tr>
<tr>
<td>Themed</td>
<td>8.0730*** (1.6820)</td>
</tr>
<tr>
<td>Themed * ln(Size)</td>
<td>-2.8609*** (0.5636)</td>
</tr>
<tr>
<td>Themed * [ln(Size)]²</td>
<td>0.2503*** (0.0474)</td>
</tr>
<tr>
<td>% graduate, 4-year cohort</td>
<td>-0.0035** (0.0017)</td>
</tr>
<tr>
<td>% graduate, 4-year cohort * ln(Size)</td>
<td>0.0003 (0.0003)</td>
</tr>
<tr>
<td>SAT score</td>
<td>0.0007*** (0.0002)</td>
</tr>
<tr>
<td>SAT score * ln(Size)</td>
<td>-0.0001*** (0.0000)</td>
</tr>
<tr>
<td>% taking SAT</td>
<td>-0.0065* (0.0037)</td>
</tr>
<tr>
<td>% cohort passing Math, 8th grade</td>
<td>0.0004 (0.0003)</td>
</tr>
<tr>
<td>Student characteristic variables</td>
<td>Yes</td>
</tr>
<tr>
<td>Observations</td>
<td>1200</td>
</tr>
<tr>
<td>R-squared</td>
<td>0.78</td>
</tr>
</tbody>
</table>

Dependent variables measured in natural logs. Model includes year effects and borough effects. * significant at 10%; ** significant at 5%; *** significant at 1%.

Indicators for missing independent variable data (not shown) are included in regression analyses. Student characteristic variables included but not shown: percent Asian, black, Hispanic, female, eligible for free lunch, limited English proficient, recent immigrant, and in part-time special education.
Motivated in part by the difference in the estimated economies of size in previous regressions for schools with different missions, we turn next to estimated cost functions that separate themed schools from comprehensive schools. This also allows us to run a series of simulations that translate our results into a policy relevant understanding of the interplay among school size, costs, and mission.

Table 5 shows the results of separate equations for comprehensive (columns 1-3) and for themed schools (columns 4-6). Models in columns (1) and (4) are estimated with borough effects, models in columns (2) and (5) are estimated with school fixed effects, and columns (3) and (6) are estimated using random effects.\textsuperscript{20}

\textsuperscript{20} Schools do not change boroughs and thus both fixed effects cannot be included.
Table 5: Cost Regression Results for Comprehensive and Themed High Schools, Continuous Size, by School Type, 1996 to 2003

<table>
<thead>
<tr>
<th>Variable</th>
<th>Comprehensive</th>
<th>Themed</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(1)</td>
<td>(2)</td>
</tr>
<tr>
<td>Constant</td>
<td>9.9563***</td>
<td>11.3642***</td>
</tr>
<tr>
<td></td>
<td>(0.5342)</td>
<td>(0.7421)</td>
</tr>
<tr>
<td>ln(Size)</td>
<td>-0.3814**</td>
<td>-0.4588**</td>
</tr>
<tr>
<td></td>
<td>(0.1557)</td>
<td>(0.2186)</td>
</tr>
<tr>
<td>ln(Size)^2</td>
<td>0.0191*</td>
<td>0.0028</td>
</tr>
<tr>
<td></td>
<td>(0.0113)</td>
<td>(0.0166)</td>
</tr>
<tr>
<td>Graduation rate</td>
<td>-0.0046**</td>
<td>-0.0073*</td>
</tr>
<tr>
<td></td>
<td>(0.0020)</td>
<td>(0.0041)</td>
</tr>
<tr>
<td>Graduation rate * ln(Size)</td>
<td>0.0006**</td>
<td>0.0013**</td>
</tr>
<tr>
<td></td>
<td>(0.0003)</td>
<td>(0.0006)</td>
</tr>
<tr>
<td>SAT score</td>
<td>0.0002</td>
<td>0.0003**</td>
</tr>
<tr>
<td></td>
<td>(0.0002)</td>
<td>(0.0001)</td>
</tr>
<tr>
<td>SAT score * ln(Size)</td>
<td>-0.0000*</td>
<td>-0.0000**</td>
</tr>
<tr>
<td></td>
<td>(0.0000)</td>
<td>(0.0000)</td>
</tr>
<tr>
<td>% taking SAT</td>
<td>0.0004</td>
<td>-0.0004</td>
</tr>
<tr>
<td></td>
<td>(0.0006)</td>
<td>(0.0004)</td>
</tr>
<tr>
<td>% cohort passing Math, 8th grade</td>
<td>-0.0001</td>
<td>-0.0006*</td>
</tr>
<tr>
<td></td>
<td>(0.0004)</td>
<td>(0.0003)</td>
</tr>
</tbody>
</table>

Student characteristic variables | Yes | Yes | Yes | Yes | Yes | Yes |
Borough fixed effects            | Yes | No  | No  | Yes | No  | No  |
School fixed effects             | No  | Yes | No  | No  | Yes | No  |
Random school effects            | No  | No  | Yes | No  | No  | Yes |
Observations                     | 933 | 933 | 933 | 267 | 267 | 267 |
R-squared                        | 0.81 | 0.94 | 0.76 | 0.74 | 0.89 | 0.65 |

Dependent variable measured in natural logs. Models include year effects. Robust standard errors in parentheses.
* significant at 10%; ** significant at 5%; *** significant at 1%

Specialized and Vocational schools removed as explained in the text. Indicators for missing independent variable data (not shown) are included in regression analyses. Student characteristic variables included but not shown: percent Asian, black, Hispanic, female, eligible for free lunch, limited English proficient, recent immigrant, and in part-time special education.

All models yield cost parameters that suggest positive fixed costs, with dropping then rising marginal costs and U shaped cost functions. Most broadly, both because of their consistency with theory and literature and their success with inclusion of fixed and random effects, we view the results in Table 5 as the best in this study. Note that while there are important differences between the models estimated for the themed schools and the comprehensive schools, the point estimates do not seem sensitive to the specification chosen. To be specific, within each of the school types, there is considerable similarity in the point estimates between the models – borough effects, school fixed effects, and random effects specifications yield results that are broadly similar, suggesting that the bias due to unobserved differences
in schools may not be problematic.\footnote{We also estimate the equations in Table 5 weighting by enrollment as a way to counter possible heteroskedasticity. The results are qualitatively similar, although a few more coefficients in the fixed and random effects versions show significance.} Coefficients on outputs, when statistically significant, demonstrate either a main effect that increases costs and a smaller, interacted effect with size that shows a decline as size increases (or the reverse). Together these cost equations appear to capture well the relationships between enrollments, outputs, student characteristics, and costs per pupil. Further, when significant, coefficients on student characteristics are similar to those found in the other estimates e.g., poor and limited English students are associated with higher costs.

The key question in this study is: should schools be larger or smaller and, if so, how much? The response to this question must take into account our findings from the estimated cost functions that mission matters – the cost structures, both fixed and marginal, are different for themed and comprehensive schools.

Cost Simulations

For policy purposes, it is important to understand the implications of size-cost relationships in terms of the current and optimal (cost minimizing) size of schools. Simulations allow us to do this. Furthermore, given that the goal of current high school reforms in general and small school reform in particular is to increase student achievement, simulations that increase outputs provide a benchmark to assess optimal school size and related costs. Thus, the simulations could help guide the development of a system of high schools that is cost effective or, at a minimum, help understand the trade offs of school size, costs and effectiveness.

For ease of exposition we focus the remainder of our discussion on simulations that use the estimated coefficients from the random effects models in columns (3) and (6) of Table 5, both because these are the theoretically most appealing and because the random effects specification allows for sharper point estimates of the coefficients. We use all coefficient estimates, regardless of their individual
statistical significance. For the simulations, we assume that comprehensive and themed schools remain unchanged, on average, in terms of the students they serve. In other words, across the system of high schools, students attend comprehensive and themed schools in the same patterns as they do in 2003. Using each school type’s “own students,” we then estimate costs for two different output levels; a) current (2003) average outputs for each type and b) aspirational outputs that are equal for the two types and that are higher than the current output of schools – 90% graduation rate and 1000 combined SAT score. Intuitively, the elasticity of costs with regard to size depends upon the quality of the outputs – say, the graduation rate – so that the optimal school size (e.g. the cost minimizing school size) will vary with the graduation rate. For example, a low graduation rate may mean costs are minimized at a large size while a high graduation rate might be cheaper to accomplish in a small school.

Figure 1 graphs the cost curves of comprehensive and themed high schools based on the average mix of students and average output levels, respectively, for each type of high school. Within the actual range of school enrollment in NYC, costs generally decrease with enrollment for comprehensive schools, but decline and then increase (a U-shaped relationship) for themed schools. There are diminishing returns to size for comprehensive high schools, which suggest cost minimization outside the actual range of school sizes observed. At the cost-minimizing point for comprehensive high schools, however, marginal cost reductions due to changes in enrollments are extremely small and do not change much over large spans of enrollment (e.g., moving from 4250 to 4500 students generates a cost savings of $27 per pupil). In other words, enrolling one more student may reduce costs for the average comprehensive school (which is below its optimal size), but those cost savings are small, thus making the optimal school size of comprehensive schools irrelevant for policymakers and for our analysis.

---

22 Joint F tests on outputs and on student characteristics show significance at less than 7% in all cases.
23 A second set of simulations, in contrast, that relaxes the assumption that students attend comprehensive and themed schools in the same patterns as in 2003, did not yield results that differed substantively from the first set of simulations. Thus, we focus our discussion on the first set and report results at key enrollment points for both sets in Appendix C.
24 That is, the first derivatives are a function of the output levels.
The key sizes at which we indicate costs in Figure 1 include the comprehensive maximum size in 2003 (4,204 students), the comprehensive average size in 2003 (1,551), the themed optimal size in 2003 (500), and the themed average size in 2003 (373). Each of these key enrollment points is noted with a vertical line in Figure 1. At their respective average size, comprehensive schools cost less than themed schools - $7,283 versus $8,594 for a difference of $1,311 per pupil – but both types of schools are currently operating below their cost-minimizing size. At their maximum observed size of 4,202 comprehensive high schools costs per pupil are $6,554 or $729 less than at their average size. At the themed optimal size of 500 students, costs per pupil are $8,401 or $193 less than at their average size.

25 See Appendix Table C for the simulated cost estimates for the key enrollment points.
Most notable, perhaps, is that comprehensive schools at either average or maximum observed sizes cost less than even optimally sized themed schools.

Clearly, the main impetus for the major reform initiatives of the past decade, be it higher standards and accountability or the creation of small schools, is to increase school outputs. In Figure 2, we examine the relationship of costs to school size by simulating costs for comprehensive and themed schools of varying sizes when graduation rates and SAT scores are raised to aspirational levels. The general shapes of the cost curves for comprehensive and themed schools are similar to those seen in Figure 1 with two notable exceptions. First, the slope of the cost curve for comprehensive schools is flatter at aspirational outputs levels than at average output levels. Second, the slope of themed school costs is steeper with marginal cost savings greater up to the optimal size at aspirational output levels than average output levels.
Moreover, at aspirational levels, the optimal size of themed schools is 647, which is 29% larger than the optimal size at average output levels (500) and 73% larger than the actual average size (373). Increasing outputs to aspirational levels will increase the costs per pupil in comprehensive schools, whereas for themed schools costs decrease when outputs are increased. Two possible explanations of this result for themed schools seem relevant. First, this may reflect the extent to which themed schools aim at producing outputs other than those captured here – four-year graduation rates, SAT scores, etc – such as
increased college attendance or more creative students. A second possible explanation lies in understanding the school enrollment decisions of students who have not graduated on time, that is, within the expected four years. These students may drop out of school entirely or continue to attend for as long as three additional years and, in fact, a significant portion of New York City’s students graduate in five, six or seven years, rather than four years. Thus, if themed schools keep more students for a fifth, sixth or seventh year, then increasing the four-year graduation rate may lower costs because it reflects a decrease in the seven-year graduation rate. Put differently, the explanation may lie in the differences in the length of time it takes students in themed and comprehensive schools to graduate. In themed schools, a lower percent of student graduate in under four years, while a greater percent of students graduate in 5-7 years compared to comprehensive schools. Therefore, the more students themed schools graduate in 4 years, the lower their costs. In some sense, both of these explanations point to some unobserved additional output that we have not included. Although we have included more outputs than previous studies, it seems clear that future work with a richer set of outputs is warranted.

In summary, at key enrollment points, whether at the respective average output levels or aspirational levels, comprehensive schools cost less per pupil than themed schools. While there are cost savings that could be generated by making comprehensive high schools larger on average, arguably the more policy relevant finding from Figures 1 and 2 is that themed schools could lower their costs by increasing their size to optimal levels that would still be less than half the size of the average comprehensive school. Alternatively, if policymakers wish to break up large high schools to create small schools, then our findings imply that those small schools would need to become themed to minimize costs.

26 This might be particularly relevant for those schools founded as alternatives to the traditional schools in the earliest wave of small schools, but less relevant for the newer schools that may have a more traditional academic focus.
Conclusions

A growing number of studies of the effects of high school size on various outputs indicate that smaller high schools result in better outputs. Only a few studies include costs along with outputs when studying the effect of school size. Yet cost-effectiveness in school reform is an essential analytic component, especially in large urban school districts with many competing ideas for reform and few ways to garner additional resources. Our analysis suggests that direct costs per pupil generally decline with size for all types of high schools. Importantly, moving to (small) themed schools from (large) comprehensive schools as they exist now will cost less per pupil as outputs increase. In particular, there could be cost savings for themed schools if they graduate more students in 4 years than 5-7 years.

Decreasing school size, however, is not enough -- our findings show that small comprehensive high schools are expensive. If policymakers were to decrease school size and split comprehensive high schools into smaller schools, all they would accomplish is an increase in costs. The key to making small schools effective is to make them themed. While it is beyond the scope of this study to examine whether schools with particular themes are more or less costly in relations to size and outputs, it is important to better understand what it is about themed schools that does matter. Themed schools tend to have narrower course offerings in math, English and foreign languages with fewer Advanced Placement offerings as well. While this may be a limitation, it may also be an opportunity for more heterogeneity in classrooms within a more restricted range of offerings. Given that themed schools enroll students who are more difficult to educate, it is all the more impressive that themed small schools approach the costs of comprehensive schools at a certain point.

Our study finds that both size and mission matter, which is an important consideration for policymakers as they continue to seek ways to improve the educational outcomes of high school students. The pursuit of a singularly focused policy, such as creating small school without consideration of mission, will not produce the most cost-effective outcome. A more realistic approach would be to pursue a mix of
schools in terms of both size and mission, understanding that the optimal size of both themed and comprehensive schools is larger than the average size of existing schools.
References


### Appendix A: Definitions of Small, Medium, and Large School Sizes from the Literature

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Small</td>
<td>LE 500</td>
<td>LE 500</td>
<td>0-600</td>
<td>LT 300</td>
<td>220-550</td>
<td>LE 300, 301-600</td>
</tr>
<tr>
<td>Medium</td>
<td>NA</td>
<td>NA</td>
<td>600-1,200; 1,200-2,000</td>
<td>300-599, 600-899</td>
<td>550-1800, 1800-3199</td>
<td>601-901, 901-1,200</td>
</tr>
<tr>
<td>Large</td>
<td>NA</td>
<td>NA</td>
<td>GT 2,000</td>
<td>GE 900</td>
<td>GT 3200</td>
<td>1,201-1,500, 1,501-1,800, 1,801-2,100, and GT 2,100</td>
</tr>
<tr>
<td>Geographic area</td>
<td>NYC</td>
<td>NA</td>
<td>NYC</td>
<td>Nat'l.</td>
<td>TX</td>
<td>Nat'l. sample (NELS)</td>
</tr>
</tbody>
</table>

- **NYC DOE; IESP Small Schools (Weinstein)**
- **Gates Foundation (Gootman, 2005)**
- **Stiefel et al, 2000**
- **NCES, 2003**
- **Bickel et al, 2001**
- **Lee and Smith, 1997**
Appendix B: School-Based Expenditure Reports (SBER) Functional Categories (2003)

Total (Sum of I, II, III & IV)
I. Direct Services (SUM of A, B, C, D, E, and F)
   A. Classroom Instruction
      1. Teachers
      2. Educational Para-professionals
      3. Other Classroom Staff
      4. Text Books
      5. Librarians and Library Books
      6. Instructional Supplies & Equipment
      7. Professional Development
      8. Curriculum Development
      9. Contracted Instruction
     10. Summer/Eve School
   B. Instructional Support Services
      1. Counseling Services
      2. Attendance & Outreach
      3. Related Services
      4. Drug Prevent Programs
      5. Referral/Evaluation
      6. After School & Student Activities
      7. Parent Involvement
   C. Leadership/Supervision/Support
      1. Principals
      2. Assistant Principals
      3. Supervisors
      4. Secretaries & School Aides
      5. Supplies, Materials, Equipment & Telephone
   D. Ancillary Support Services
      1. Food Services
      2. Transportation
      3. School Safety
      4. Computer System Support
   E. Building Services
      1. Custodial Services
      2. Building Maintenance
      3. Leases
      4. Energy
   F. District Support
      1. Unscheduled Sums/Carry
II. District/Superintendent Costs (Sum A and B)
   A. Instructional Support and Administration
   B. Other Districts and Borough Costs
      1. Sabbaticals, Leaves and Termination Pay
      2. Additions to Regular Salary
      3. Projected Expenses
III. System wide Costs (Sum of A and B)
   A. Central Instructional Support
   B. Central Administration
      1. Instruct Offices
      2. Operational Offices
      3. Central and Chancellor’s Offices
IV. Other System wide Obligations
A. Other System wide Obligations
   1. Debt Service
   2. Retiree Health/Welfare
   3. Special Commissioner for Investigations
   4. Projected Expenses

Our dependent variable 'modified direct costs' is comprised of Direct Services (I), excluding Building Services (I.E.) and Transportation (I.D.2.)

Expenditure data from the New York City Department of Education (DOE) are not audited. The DOE assigns all public school expenditures to specific school locations, and only those schools recognized by the Department of Education are represented in the school-based expenditure reports. Some alternative programs and schools-within-schools, for example, are not reported as separate entities in the SBERs as they are not recognized as being distinct "expenditure locations" in the DOE's data systems. Spending on these programs is attributed to the "parent" school. Expenditures were attributed directly to schools when actual school allocation data and funds to support Direct Services to schools were available. Otherwise, indirect spending (such as Central Office) was allocated to schools on a per capita basis, unless spending was for particular populations (such as special education or Title I), in which case expenditures were allocated based on appropriate enrollment figures for each school. Expenditures were classified by function within the DOE's budget structure: Unit of Appropriation, Budget Code, Quick Code, Grant, Object code/Line Number. (Technical Appendix, School-Based Expenditure Reports, 2003)
Appendix C: Simulated Cost Estimates at Key Enrollment Points

<table>
<thead>
<tr>
<th></th>
<th>Outputs</th>
<th>Comprehensive</th>
<th>Themed</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Own Students</strong></td>
<td>Comprehensive Maximum: 4,204</td>
<td>Comprehensive, 2003</td>
<td>$6,554</td>
</tr>
<tr>
<td></td>
<td>Comprehensive Average: 1,551</td>
<td>Comprehensive, 2003</td>
<td>$7,283</td>
</tr>
<tr>
<td></td>
<td>Themed Optimal: 500</td>
<td>Themed, 2003</td>
<td>$8,401</td>
</tr>
<tr>
<td></td>
<td>Themed Average: 373</td>
<td>Themed, 2003</td>
<td>$8,594</td>
</tr>
<tr>
<td><strong>Own Students</strong></td>
<td>Comprehensive Maximum: 4,204</td>
<td>Aspirational</td>
<td>$7,135</td>
</tr>
<tr>
<td></td>
<td>Comprehensive Average: 1,551</td>
<td>Aspirational</td>
<td>$7,592</td>
</tr>
<tr>
<td></td>
<td>Themed Optimal: 647</td>
<td>Aspirational</td>
<td>$7,887</td>
</tr>
<tr>
<td></td>
<td>Themed 500</td>
<td>Aspirational</td>
<td>$8,026</td>
</tr>
<tr>
<td></td>
<td>Themed Average: 373</td>
<td>Aspirational</td>
<td>$8,543</td>
</tr>
<tr>
<td><strong>Average Student</strong></td>
<td>Comprehensive Maximum: 4,204</td>
<td>Systemwide, 2003</td>
<td>$6,513</td>
</tr>
<tr>
<td></td>
<td>Comprehensive Average: 1,551</td>
<td>Systemwide, 2003</td>
<td>$7,268</td>
</tr>
<tr>
<td></td>
<td>Themed Optimal: 529</td>
<td>Systemwide, 2003</td>
<td>$8,151</td>
</tr>
<tr>
<td></td>
<td>Themed Average: 373</td>
<td>Systemwide, 2003</td>
<td>$8,419</td>
</tr>
<tr>
<td><strong>Average Student</strong></td>
<td>Comprehensive Maximum: 4,204</td>
<td>Aspirational</td>
<td>$7,149</td>
</tr>
<tr>
<td></td>
<td>Comprehensive Average: 1,551</td>
<td>Aspirational</td>
<td>$7,607</td>
</tr>
<tr>
<td></td>
<td>Themed Optimal: 647</td>
<td>Aspirational</td>
<td>$7,740</td>
</tr>
<tr>
<td></td>
<td>Themed 529</td>
<td>Aspirational</td>
<td>$7,823</td>
</tr>
<tr>
<td></td>
<td>Themed Average: 373</td>
<td>Aspirational</td>
<td>$8,383</td>
</tr>
</tbody>
</table>

Aspirational outputs include a 90% graduation rate and 1000 combined SAT score.
The Institute for Education and Social Policy of the Steinhardt School of Culture, Education, and Human Development and Robert F. Wagner School of Public Service at NYU conducts non-partisan scientific research about U.S. education and related social issues. Our research, policy studies, evaluations, seminar series, and technical assistance inform and support policy makers, educators, parents and others in their efforts to improve public schooling. More information is available on our website at http://steinhardt.nyu.edu/iesp.